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## Education Bureau

Territory-wide System Assessment 2024

## Secondary 3 Mathematics QUESTION BOOKLET

## INSTRUCTIONS

1. There are 47 questions in this paper.
2. Time allowed is 65 minutes.
3. Answer ALL questions in the separate ANSWER BOOKLET.
4. The use of HKEAA approved calculators is permitted.
5. Unless otherwise specified, numerical answers should be either exact or correct to 3 significant figures.
6. Rough work should be done on the rough work sheet provided.
7. The diagrams in this paper are not necessarily drawn to scale.

SECTION A: Choose the best answer for each question. You should mark all your answers in the ANSWER BOOKLET.

1. Which of the following is the prime factorisation of 54 ?
A. $6 \times 9$
B. $3^{2} \times 6$
C. $1 \times 2 \times 3^{3}$
D. $2 \times 3^{3}$
2. Round off 40780 to 2 significant figures.
A. 40000
B. 40700
C. 40800
D. 41000
3. $\sqrt[3]{729}=$
A. 3 .
B. 9 .
C. 27 .
D. 81 .
4. Mr Chan has $x$ boxes of batteries. There are 50 batteries in each box. He used up 2 boxes and divided the rest of the batteries into 60 packs for selling. How many batteries are in each pack?
A. $\frac{50(x-2)}{60}$ batteries
B. $\frac{50 x-2}{60}$ batteries
C. $\frac{x-2}{60}$ batteries
D. $\frac{x-50 \times 2}{60}$ batteries
5. Which of the following statements is correct?
A. The solution of $2 x+1=0$ is $\frac{1}{2}$.
B. The solution of $x+\frac{1}{2}=0$ is $\frac{1}{2}$.
C. The solution of $2 x-1=0$ is $\frac{1}{2}$.
D. The solution of $-\frac{1}{2}-x=0$ is $\frac{1}{2}$.
6. Which of the following may represent the graph of the equation $x+2 y-5=0$ ?
A.

B.

C.

D.

7. $5^{-2}=$
A. $\frac{1}{25}$.
B. -25 .
C. $\frac{1}{10}$.
D. -10 .
8. Which of the following is NOT a polynomial ?
A. $13 x+2 y$
B. $\frac{y}{13}+2 y^{2}$
C. $\frac{13}{y}+2 y$
D. $26 x y^{2}$
9. The length of a rectangle is $x \mathrm{~cm}$. Its width is 15 cm . If the perimeter of the rectangle does not exceed 200 cm , which of the following inequalities can be used to find the range of the values of $x$ ?
A. $2(x+15)<200$
B. $2(x+15)>200$
C. $2(x+15) \leq 200$
D. $2(x+15) \geq 200$
10. Garfield uses a beaker to measure the volume of a can of drink and the result is 200 mL . Find the percentage error of the measured value.
A. $4.17 \%$
B. $6.25 \%$
C. $12.5 \%$
D. $66.7 \%$

11. In the figure, the radius of sector $O A B$ is 12 cm and $\angle A O B=72^{\circ}$. Find the area of the sector. Give the answer correct to 3 significant figures.
A. $\quad 7.54 \mathrm{~cm}^{2}$
B. $\quad 15.1 \mathrm{~cm}^{2}$
C. $\quad 90.5 \mathrm{~cm}^{2}$
D. $181 \mathrm{~cm}^{2}$

12. 



A piece of paper with an area of $200 \mathrm{~cm}^{2}$ is folded into a hollow right circular cylinder without overlapping. The base diameter and the height of the cylinder are 10 cm and $h \mathrm{~cm}$ respectively. Find the value of $h$. Give the answer correct to 3 significant figures.
A. 2.55
B. 3.18
C. 6.37
D. 12.7
13. In each of the following figures, $P Q$ is a straight line. Which figure shows that $x$ and $y$ are a pair of interior angles on the same side?
A.

B.

C.

D.

14. Which of the following MAY NOT be a regular polygon?
A.

B.

C.

D.

15. In the figure, $\triangle P Q R$ is a right-angled triangle. If $P Q=21$ and $P R=29$, find $Q R$.
A. $\sqrt{29^{2}-21^{2}}$
B. $\sqrt{29^{2}+21^{2}}$
C. $29^{2}-21^{2}$
D. $29^{2}+21^{2}$

16. $P(-7,4)$ and $Q(3,-8)$ are two points in the rectangular coordinate plane. The coordinates of the mid-point of $P Q$ are
A. $(-10,12)$.
B. $(-5,6)$.
C. $(-4,-4)$.
D. $(-2,-2)$.
17. The slopes of three straight lines $L_{1}, L_{2}$ and $L_{3}$ are listed in the table below.

| Line | $L_{1}$ | $L_{2}$ | $L_{3}$ |
| :---: | :---: | :---: | :---: |
| Slope | $\frac{12}{13}$ | $-\frac{12}{13}$ | $\frac{13}{12}$ |

Which of the following is correct?
A. $L_{1} \perp L_{2}$
B. $L_{1} / / L_{3}$
C. $L_{2} / / L_{3}$
D. $L_{2} \perp L_{3}$
18. Referring to the figure, find $\theta$. Give the answer correct to 3 significant figures.
A. $28.2^{\circ}$
B. $32.4^{\circ}$
C. $57.6^{\circ}$
D. $61.8^{\circ}$

19. The table below shows the sale proportions of different types of set lunch sold in a school tuck shop on a day.

| Type of set lunch | Proportion of total number <br> of set lunches sold |
| :---: | :---: |
| A | $20 \%$ |
| B | $26 \%$ |
| C | $19 \%$ |
| D | $28 \%$ |
| E | $7 \%$ |

Which of the following is the most suitable for presenting the data above?
A. Pie chart
B. Histogram
C. Stem-and-leaf diagram
D. Cumulative frequency polygon
20. The following table shows the personal vaccination history and the corresponding frequency of people who reserved a booking at a vaccination clinic yesterday.

| Vaccination history | Never vaccinated | Received <br> 1 dose to 3 doses <br> of vaccine | Received <br> more than 3 doses <br> of vaccine |
| :---: | :---: | :---: | :---: |
| Frequency | 1 | 497 | 2 |

According to the table above, find the relative frequency of the people who received 1 dose or more of vaccine.
A. $\frac{1}{500}$
B. $\frac{2}{500}$
C. $\frac{497}{500}$
D. $\frac{499}{500}$

SECTION B: Write ALL the answers in the ANSWER BOOKLET. Working need not be shown.
21. Calculate $200 \div[25-(1+7 \times 2)]$.
22. Calculate $\frac{-1-2(-8)}{-3}$.
23. A restaurant sold 1344 lunch sets today. It is $12 \%$ more than the number of lunch sets sold yesterday. Find the number of lunch sets sold by the restaurant yesterday.
24. In each of the following situations, determine whether the relationship between $x$ and $y$ is direct proportion or inverse proportion.
(i) A bottle of soft drink is divided into $x$ cups equally. Each cup has $y \mathrm{~mL}$.
(ii) A ticket for a theme park is sold at $\$ 200$. Wilson pays $\$ y$ to buy $x$ tickets.
25. A fruit shop sold 150 apples and mangoes in total, 70 of which were mangoes. Find the ratio of the number of apples to the number of mangoes sold.
26. The diameter of the pollen of a plant is about 0.00004 m . Use scientific notation to represent the diameter.
27. Expand $(x+2)(3 x-5)$.
28. Factorise $2 x^{2}+7 x+3$.
29. Factorise $x^{2}-2 x+1$.
30. Consider the formula $a=\frac{f^{2}}{m+n}$. If $f=5, m=9$ and $n=3$, find the value of $a$.
31. Solve the inequality $2 x \leq-8$.
32. The figure shows Solids $P, Q$ and $R$. If each surface of the solids is either a square or an equilateral triangle, which of the following solids can satisfy ALL descriptions below?
(May be more than one answer)
I. It is a prism.
II. It is a right solid.


Solid $Q$


Solid $R$

33. Use the given letters to represent the quadrilateral shown in the figure.

34. In the figure, $\triangle A B C \cong \triangle D E F$. Find
(a) the value of $m$,
(b) the value of $n$.

35.


Which of the following triangles MUST be similar to $\triangle A B C$ as shown in the above figure?
(May be more than one answer)


Triangle $Q$


Triangle $R$

36. In the figure, $A B C D$ is a parallelogram. It is given that $A C$ is the diagonal, $\angle B C A=58^{\circ}$ and $\angle B A C=60^{\circ}$. Find $x$.

37. The stem-and-leaf diagram below shows the scores a basketball team got in each match last year.

Scores of a basketball team got in each match last year

| Stem (10) | Leaf (1) |  |  |  |  |  |  |  |
| ---: | ---: | :--- | :--- | :--- | :--- | :--- | :--- | :---: |
| 4 | 0 | 3 |  |  |  |  |  |  |
| 5 | 4 | 7 | 9 | 9 |  |  |  |  |
| 6 | 1 | 2 | 4 | 6 | 8 | 8 | 8 |  |
| 7 | 1 | 3 | 3 | 7 | 9 |  |  |  |
| 8 | 0 | 8 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |

According to the above stem-and-leaf diagram, answer the following questions.
(a) How many matches did the basketball team play last year?
(b) What was the lowest score the basketball team got in the matches last year?
(c) Find the median score the basketball team got in the matches last year.
38. The cumulative frequency curve below shows the distribution of time spent on physical exercise by all students of a school last week.


According to the above diagram, answer the following questions.
(a) How many students does the school have?
(b) What was the number of students who spent less than 3 hours on physical exercise last week?
39. The following table shows the price indices and their corresponding weight of the four types of household expenditure (clothing, food, housing and transport) of a city in the previous year.

|  | Household expenditure |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Clothing | Food | Housing | Transport |
| Price index | 42 | 53 | 68 | 38 |
| Weight | $15 \%$ | $30 \%$ | $40 \%$ | $15 \%$ |

Find the weighted mean price index of these four types of household expenditure of the city in the previous year.

SECTION C: All working must be clearly shown.
Write the mathematical expressions, answers and statements/conclusions in the spaces provided in the ANSWER BOOKLET.
40. Peter deposits $\$ 5000$ in a bank. After 4 years, he will receive simple interest of $\$ 1000$. Find the annual interest rate.
41. Complete the table for the equation $y=\frac{3 x-8}{4}$ in the ANSWER BOOKLET.

| $x$ | -4 | 0 | 4 |
| :---: | :---: | :---: | :---: |
| $y$ |  | -2 |  |

According to the table, plot the graph of this equation on the rectangular coordinate plane given in the ANSWER BOOKLET.
42. (a) Simplify $\left(x^{5}\right)^{3}$ and express the answer with positive index.
(b) Simplify $x^{-2}\left(x^{5}\right)^{3}$ and express the answer with positive index.
43. In the figure, the radius of sector $O A B$ is 10 cm and $\angle A O B=140^{\circ}$. Let $x$ be the arc length of the sector, find $x$. Give the answer correct to 3 significant figures.

44. In the figure, Solid $A$ and Solid $B$ are similar and the total surface areas are $200 \mathrm{~cm}^{2}$ and $1800 \mathrm{~cm}^{2}$ respectively. Their bases are circles. The base diameter of Solid $B$ is 12 cm . Find the base diameter of Solid $A$.

$\longleftrightarrow$

Solid $A$


Solid $B$
45. In the figure, $A E B$ and $F E D$ are straight lines. It is given that $\angle E C D=42^{\circ}, \angle C E D=73^{\circ}$ and $\angle F E B=115^{\circ}$. Prove that $A B / / C D$.

46. The following frequency distribution table shows the recovery time of 35 patients suffering from influenza.

| Recovery time <br> (hours) | $1-24$ | $25-48$ | $49-72$ | $73-96$ | $97-120$ | $121-144$ | $145-168$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 1 | 4 | 9 | 11 | 5 | 3 | 2 |

(a) According to the above table, complete the cumulative frequency distribution table in the ANSWER BOOKLET.
(b) Construct a cumulative frequency polygon in the ANSWER BOOKLET to represent the above data.
47. The following shows the monthly electricity consumption (kWh) of a company last year. $4300,5300,5800,6300,6600,7200,7300,8100,9100,11600,11700,12700$

It is given that the mean of the monthly electricity consumption of the company last year was 8000 kWh . Hence, the manager claimed, "Last year, over half of the monthly electricity consumptions were more than 8000 kWh ."
Do you agree with the manager? Explain your answer.

END OF PAPER

## Do not write on this page.

Answers written on this page will not be marked.
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