## $\mathbf{9} \mathbf{M E} \mathbf{4}$ ( $\mathbf{Q}$ )

## Education Bureau

Territory-wide System Assessment 2024

## Secondary 3 Mathematics QUESTION BOOKLET

## INSTRUCTIONS

1. There are 47 questions in this paper.
2. Time allowed is 65 minutes.
3. Answer ALL questions in the separate ANSWER BOOKLET.
4. The use of HKEAA approved calculators is permitted.
5. Unless otherwise specified, numerical answers should be either exact or correct to 3 significant figures.
6. Rough work should be done on the rough work sheet provided.
7. The diagrams in this paper are not necessarily drawn to scale.

SECTION A: Choose the best answer for each question. You should mark all your answers in the ANSWER BOOKLET.

1. Which of the following is the prime factorisation of 54 ?
A. $6 \times 9$
B. $3^{2} \times 6$
C. $1 \times 2 \times 3^{3}$
D. $2 \times 3^{3}$
2. Round off 40780 to 2 significant figures.
A. 40000
B. 40700
C. 40800
D. 41000
3. $(-x)^{2}+\left(-x^{2}\right)=$
A. 0 .
B. $-x^{4}$.
C. $2 x^{2}$.
D. $-2 x^{2}$.
4. Which of the following statements is correct?
A. The solution of $2 x+1=0$ is $\frac{1}{2}$.
B. The solution of $x+\frac{1}{2}=0$ is $\frac{1}{2}$.
C. The solution of $2 x-1=0$ is $\frac{1}{2}$.
D. The solution of $-\frac{1}{2}-x=0$ is $\frac{1}{2}$.
5. Which of the following may represent the graph of the equation $x+2 y-5=0$ ?
A.

B.

C.

D.

6. The number of $\$ 2$ coins and $\$ 5$ coins in a cash box are $x$ and $y$ respectively. The total amount of the coins is $\$ 300$. It is given that the number of $\$ 5$ coins is 11 more than that of $\$ 2$ coins. Which of the following pairs of simultaneous equations shows the relations between $x$ and $y$ ?
A. $\left\{\begin{array}{l}x+y=300 \\ x=11+y\end{array}\right.$
B. $\left\{\begin{array}{l}x+y=300 \\ y=11+x\end{array}\right.$
C. $\left\{\begin{array}{l}2 x+5 y=300 \\ x=11+y\end{array}\right.$
D. $\left\{\begin{array}{l}2 x+5 y=300 \\ y=11+x\end{array}\right.$
7. $5^{-2}=$
A. $\frac{1}{25}$.
B. -25 .
C. $\frac{1}{10}$.
D. -10 .
8. Determine whether each of the following is factorisation or expansion.

| (i) | $(3 x-1)(x-2)(x+4)$ <br> $=3 x^{3}+5 x^{2}-26 x+8$ | (ii) | $3 x^{3}+5 x^{2}-26 x+8$ <br> $=(3 x-1)(x-2)(x+4)$ |
| :---: | :---: | :---: | :---: |

A. (i) Expansion
(ii) Expansion
B. (i) Factorisation
(ii) Expansion
C. (i) Expansion
(ii) Factorisation
D. (i) Factorisation
(ii) Factorisation
9. $x+\frac{1}{3 x}=$
A. $\frac{1}{3}$.
B. $\frac{x+1}{3 x}$.
C. $\frac{3 x^{2}+1}{3 x}$.
D. $\frac{9 x^{2}+1}{3 x}$.
10. If $x \leq 5$, which of the following CANNOT be a value of $x$ ?
A. -5
B. 0
C. 5
D. 6
11. Kenny weighs 72 kg (correct to the nearest kg ). Which of the following could be his actual weight?
A. $\quad 71.4 \mathrm{~kg}$
B. $\quad 71.5 \mathrm{~kg}$
C. 72.5 kg
D. $\quad 72.6 \mathrm{~kg}$
12. In the figure, the radius of sector $O A B$ is 12 cm and $\angle A O B=72^{\circ}$. Find the area of the sector. Give the answer correct to 3 significant figures.
A. $\quad 7.54 \mathrm{~cm}^{2}$
B. $\quad 15.1 \mathrm{~cm}^{2}$
C. $90.5 \mathrm{~cm}^{2}$
D. $181 \mathrm{~cm}^{2}$

13. A regular circular cone is placed horizontally as shown. Stephen sketches a section which is perpendicular to the base and passing through vertex $V$.


Which of the following can be the plane diagram of the section?
A.

B.

C.

D.

14. In the figure, $A B$ is a straight line. $x$ and $y$ are
A. alternate interior angles.
B. vertically opposite angles.
C. corresponding angles.
D. interior angles on the same side.

15.


Which of the following triangles MAY NOT be congruent to $\triangle P Q R$ shown above?
A.

B.

C.
17

D.

16. Which of the following pairs of triangles must NOT be similar?
A.

B.

C.

D.

17. In the rectangular coordinate plane, $A(4,8)$ and $B(12,6)$ are two points on a straight line $L$. The slope of $L=$
A. $\frac{8-6}{12-4}$.
B. $\frac{6-8}{12-4}$.
C. $\frac{12-6}{4-8}$.
D. $\frac{12-4}{6-8}$.
18. Find the value of $\cos \theta$ in the figure.
A. $\frac{72}{65}$
B. $\frac{72}{97}$
C. $\frac{65}{72}$
D. $\frac{65}{97}$

19. The table below shows the sale proportions of different types of set lunch sold in a school tuck shop on a day.

| Type of set lunch | Proportion of total number <br> of set lunches sold |
| :---: | :---: |
| A | $20 \%$ |
| B | $26 \%$ |
| C | $19 \%$ |
| D | $28 \%$ |
| E | $7 \%$ |

Which of the following is the most suitable for presenting the data above?
A. Pie chart
B. Histogram
C. Stem-and-leaf diagram
D. Cumulative frequency polygon
20. A university conducted a test for dehumidifiers. The table below shows the score and the weight of each testing criterion for a model of dehumidifier.

|  | Testing criterion |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Daily <br> dehumidification <br> capacity | Energy <br> efficiency | Sound <br> level | Air purification <br> performance |
| Score | 87 | 94 | 69 | 50 |
| Weight | 40 | 40 | 10 | 10 |

Find the weighted mean score of the model of dehumidifier.
A. 25
B. 28.1
C. 75
D. 84.3

SECTION B: Write ALL the answers in the ANSWER BOOKLET. Working need not be shown.
21. Express $11 \times 11 \times 11$ as a power .
22. A country used directed numbers to represent the number of tourists arriving or leaving a city. For example, -5000 represents that there are 5000 tourists leaving a city.

Use a directed number to represent each of the following situations.
(i) There are 8000 tourists arriving in city A.
(ii) There are 2000 tourists leaving city B.
23. If $\sqrt{a}=16$, find the value of $a$.
24. The cost of a tablet computer is $\$ 5200$. If it is sold at a loss of $25 \%$, find the selling price of the tablet computer.
25. A fruit shop sold 150 apples and mangoes in total, 70 of which were mangoes. Find the ratio of the number of apples to the number of mangoes sold.
26. The $n$th term of a sequence is $\frac{n+1}{n+2}$. Find the value of the 5 th term of the sequence.
27. Write down the power of the polynomial $5 x^{3}-8 x^{2}+9 x-7$.
28. Expand $(x+2)(3 x-5)$.
29. Factorise $x^{2}-2 x+1$.
30. Consider the formula $a=\frac{f^{2}}{m+n}$. If $f=5, m=9$ and $n=3$, find the value of $a$.
31. Solve the inequality $2 x \leq-8$.
32. The height of a right prism is 12 cm . The base of the right prism is a parallelogram. The base and the height of the parallelogram are 15 cm and 10 cm respectively. Find the volume of the prism.
33. The figure shows $\triangle A B C$ and its exterior angles . Find $x$.

34. In the figure, $B C D$ is a straight line. $\triangle A B D$ and $\triangle C A D$ are isosceles triangles, where $A B=A D$ and $C A=C D$. It is given that $\angle A C B=84^{\circ}$. Find $x$.

35. In the figure, $A B C D$ is a rectangle. $E$ is the point of intersection of the diagonals $A C$ and $B D$. Find $x$.

36. In the figure, the bearing of $P$ from $O$ is $\mathrm{S} 67^{\circ} \mathrm{W}$. Find the bearing of $Q$ from $O$.

37. The stem-and-leaf diagram below shows the scores a basketball team got in each match last year.

> Scores of a basketball team got in each match last year

| Stem (10) | Leaf(1) |  |  |  |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| 4 | 0 | 3 |  |  |  |  |  |  |
| 5 | 4 | 7 | 9 | 9 |  |  |  |  |
| 6 | 1 | 2 | 4 | 6 | 8 | 8 | 8 |  |
| 7 | 1 | 3 | 3 | 7 | 9 |  |  |  |
| 8 | 0 | 8 |  |  |  |  |  |  |

According to the above stem-and-leaf diagram, answer the following questions.
(a) How many matches did the basketball team play last year?
(b) What was the lowest score the basketball team got in the matches last year?
(c) Find the median score the basketball team got in the matches last year.
38. The following data shows the results (m) of 8 athletes in a long jump competition.

$$
3.5, \quad 3.6, \quad 4.2, \quad 4.4, \quad 4.8, \quad 5.3, \quad 3.5, \quad 3.5
$$

Find the mean and the median of the above data.
39. Wilson throws three coins at the same time. He conducted this experiment 100 times and the outcomes are shown as follows:

| Outcome | No coins <br> face up | Only 1 coin <br> faces up | Only 2 coins <br> face up | 3 coins <br> face up |
| :---: | :---: | :---: | :---: | :---: |
| Frequency | 9 | 43 | 40 | 8 |

Find the relative frequency of Wilson having 2 coins facing up only.

SECTION C: All working must be clearly shown. Write the mathematical expressions, answers and statements/conclusions in the spaces provided in the ANSWER BOOKLET.
40. Mr Chan plans to spend $\$ 500$ to buy 3 gifts. The prices of the gifts are $\$ \underline{202}, \$ \underline{256}$ and $\$ \underline{101}$ respectively.
Based on the description above, give an appropriate approximation for each UNDERLINED VALUE. Hence, estimate the total amount spent buying the gifts. Briefly, explain whether Mr Chan has enough money to buy these 3 gifts.
41. It is given that 0.05 L of paint can cover an area of $1 \mathrm{~m}^{2}$. Mr Lam wants to paint a wall with a total area of $150 \mathrm{~m}^{2}$. The capacity of a tin of paint is 1.25 L . How many $\operatorname{tin}(\mathrm{s})$ of paint does he need?
42. Complete the table for the equation $y=\frac{3 x-8}{4}$ in the ANSWER BOOKLET.

| $x$ | -4 | 0 | 4 |
| :---: | :---: | :---: | :---: |
| $y$ |  | -2 |  |

According to the table, plot the graph of this equation on the rectangular coordinate plane given in the ANSWER BOOKLET.
43. In the figure, the base of a right triangular prism is a right-angled triangle. The volume of the prism is $420 \mathrm{~cm}^{3}$. Find the value of $x$.

44. In the figure, $A D C$ is a straight line. $\triangle A B C$ is a right-angled triangle, where $\angle A B C$ is the right angle. It is given that $A C \perp B D$ and $\angle A C B=\angle A B D$. Prove that $\triangle A B C \sim \triangle A D B$.

45. Kelly walks due south for 76 m from $A$ to $P$ while John walks 95 m from $A$ to $Q$. If $Q$ is due west to $P$, find the distance between $P$ and $Q$.

46. In the figure, a roller coaster train travels from point $A$ to point $B$ which is on the horizontal ground. The distance between point $A$ and point $B$ is 155 m . The angle of depression of point $B$ from point $A$ is $20^{\circ}$. It is given that the vertical distance between point $A$ and the horizontal ground is $x$. Find $x$. Give the answer correct to 3 significant figures.

47. The table below shows the distribution of weight $(\mathrm{kg})$ of 40 watermelons.

| Weight (kg) | $3.0-3.9$ | $4.0-4.9$ | $5.0-5.9$ | $6.0-6.9$ |
| :---: | :---: | :---: | :---: | :---: |
| Frequency | 4 | 8 | 16 | 12 |

(a) According to the above table, complete the frequency distribution table in the ANSWER BOOKLET.
(b) Find the mean weight of these 40 watermelons.

## Do not write on this page.

Answers written on this page will not be marked.
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